# St John's CE Primary School 

Progression in Skills with Associated Reasoning
KS1-KS2
Adapted from NCETM Guidance

Fractions including Decimals and
Percentages
(includes Ready to Progress Criteria)


## Vocabulary Progression

The following section of this document lists mathematical vocabulary and phrases that children are required to understand and use as they move through the school for this strand of Mathematics. It is based on the published 2014 national curriculum, NCETM guidance and White Rose Maths. It lists the new vocabulary in the year in which it should be explicitly used and taught. Vocabulary from previous year group should be referred to in addition to that for each year group. It is designed to assist with the teaching of vocabulary across EYFS, KS1 and KS2 and is aligned with the White Rose schemes of learning. This document identifies in which year group vocabulary should be explicitly taught and introduced. However, language should be revisited in subsequent year groups to ensure children are consolidating their understanding. This document is fully editable so language can be moved into earlier or later year groups where necessary in line with latest research findings and subject association (NCETM) updates. Some vocabulary might be introduced earlier (shapes for instance) if necessary or as part of an activity, however this document ensures coverage is progressive. It is expected that key vocabulary is displayed on 'Maths Learning Walls' at appropriate times during the academic year and in line with the current topic area being taught within the class and is promoted through mathematical talk in lessons.

| Vocabulary Progression |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Place Value |  |  |  |  |  |  |  |
| EYFS |  | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| Nursery | Reception |  |  |  |  |  |  |
|  |  | (One) half (one/two/three) <br> Quarters <br> Share <br> Sharing <br> Groups <br> Grouping <br> Part <br> Whole <br> Equal parts <br> Same size <br> Bar (Fraction Bar) | third (one) (two) third(s) sharing grouping two quarters equivalent one and a quarter' one and 2 quarters one and a half one and 3 quarters half as much twice as much numerator denominator fraction bar | Fifths <br> Sixths <br> Sevenths <br> Eighths <br> Ninths <br> Tenths <br> Numerator denominator <br> Fraction <br> bar <br> Order <br> Unit-fraction <br> Non-unit fraction | Hundredth(s) <br> Decimal <br> Equivalents <br> Decimal places <br> Proportion <br> Mixed number(s) | Mixed number(s) <br> Thousandths <br> Percent <br> Percentages <br> Proportion | Simplify Degrees of accuracy |

## Skills \& Reasoning Progression

The following section of this document lists mathematical skills that children should become fluent and proficient in their knowledge, understanding and application. It also includes examples of reasoning questions that could be used by teachers to encourage pupils to apply their knowledge and to reason their understanding in order to build a deeper, more complex understanding of different mathematical concepts beyond 'rote' learning or superficial understanding. It is based on the published 2014 national curriculum, NCETM guidance and White Rose Maths. It lists the new concepts that need to be taught in each year group and is aligned and arranged in order to support teachers to understand the previous step in a particular concept and also the next step (where the children have come from and should be secure with, and how this will then be applied in future year groups). This is not done to enable teachers to 'move children on' to the next year group step, hence the exemplification of reasoning questions to support teaching staff to deliver a 'depth, not breadth' approach. However, preceding steps can be used to aid the delivery of intervention support if children are not secure with the previous step of learning - this is also supported by the demarcation of 'Ready to Progress Criteria'. These are criteria that pupils must be secure with from their previous year group in order to allow them to master new content in their current year group. Links to NRich activities are also provided to enable teaching staff to link in Mathematical investigation where possible.

Development Matters does not state objectives for EYFS in Fractions, Decimals or Percentages therefore they are not shown on this document.

| Fractions - Recognise and Write |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| Recognise, find and name a half as one of two equal parts of an object, shape or quantity | recognise, find, name and write fractions ${ }^{1} /{ }_{3}$, $1 / 4^{2}{ }^{2} / 4$ and ${ }^{3} / 4$ of a length, shape, set of objects or quantity | Recognise, find and write fractions of a discrete set of objects: unit fractions and nonunit fractions with small denominators <br> * RPC - 3F-1 Interpret and write proper fractions to represent 1 or several parts of a whole that is divided into equal parts. | Count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten | Recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents (appears also in Equivalence) <br> *Begin by securing: 5NPV-1 Know that 10 tenths are equivalent to 1 one, and that 1 is 10 times the size of 0.1 . Know that 100 hundredths are equivalent to 1 one, and that 1 is 100 times the size of 0.01 . Know that 10 hundredths are equivalent to 1 tenth, and that 0.1 is 10 times the size of 0.01 . |  |


| Recognise, find and <br> name a quarter as <br> one of four equal parts <br> of an object, shape or <br> quantity | Pupils should count in <br> fractions up to 10, <br> starting from any <br> number and using <br> the $1 / 2$ and $2 / 4$ <br> equivalence on the <br> number line (Non <br> Statutory Guidance) | Count up and down in <br> tenths; recognise that <br> tenths arise from <br> dividing an object into <br> 10 equal parts and in <br> dividing one - digit <br> numbers or quantities <br> by 10. | RPC $-5 F-3$ Recall decimal <br> fraction equivalents for $1 / 21 / 4$ <br> $1 / 5$ and $1 / 10$ <br> for multiples of these proper <br> fractions. |
| :--- | :--- | :--- | :--- | :--- |


| there is the same <br> number on each half. <br> When can you do this <br> and when can't you? <br> What do you notice? | What do you notice? | What do you notice? <br> What about $1 / 10$ of <br> $20 ?$ Use this to work out <br> $2 / 10$ of 20 , etc. | How can you use this <br> to work out $6 / 10$ of <br> $200 ?$ <br> $6 / 100$ of $200 ?$ |  |
| :--- | :--- | :--- | :--- | :--- |


| Fractions - Compare | Year 2 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Year 1 |  | Year 3 <br> compare and order <br> unit fractions, and <br> fractions with the same <br> denominators |  | Year 4 <br> compare and order fractions <br> whose denominators are all <br> multiples of the same <br> number |
|  |  | compare and order <br> fractions, including <br> fractions $>1$ |  |  |


| equivalence of $2 / 4$ and $1 / 2$ | with small denominators | families of common equivalent fractions | visually, including tenths and hundredths <br> * RPC - 5F-2 Find equivalent fractions and understand that they have the same value and the same position in the linear number system. | to express fractions in the same denomination <br> * RPC - 6F-1 Recognise when fractions can be simplified, and use common factors to simplify fractions. <br> *RPC - 6F-2 Express fractions in a common denomination and use this to compare fractions that are similar in value. |
| :---: | :---: | :---: | :---: | :---: |
| Reasoning Examples - Fractions - Compare |  |  |  |  |
|  | Give an example of a fraction that is less than a half. <br> Now another example that no one else will think of. <br> Explain how you know the fraction is less than a half. (draw an image) <br> Ben put these fractions in order starting with the smallest. Are they in the correct order? One fifth, one seventh, one sixth | Give an example of a fraction that is more than a half but less than a whole. Now another example that no one else will think of. <br> Explain how you know the fraction is more than a half but less than a whole. (draw an image) | Give an example of a fraction that is more than three quarters. <br> Now another example that no one else will think of. Explain how you know the fraction is more than three quarters. <br> Imran put these fractions in order starting with the smallest. Are they in the correct order? <br> Two fifths, three tenths, four twentieths How do you know? | Give an example of a fraction that is greater than 1.1 and less than 1.5. <br> Now another example that no one will think of. Explain how you know. <br> Sam put these fractions in order starting with the smallest. Are they in the correct order? Thirty-three fifths Twenty-three thirds Forty-five sevenths How do you know? |


|  | Odd one out. <br> Which is the odd one out in this trio: $\begin{array}{lll}1 / 2 & 2 / 4 & 1 / 4\end{array}$ Why? <br> What do you notice? <br> Find $1 / 2$ of 8 . <br> Find $2 / 4$ of 8 <br> What do you notice? | Odd one out. <br> Which is the odd one out in each of these trios <br> What do you notice? <br> Find $2 / 5$ of 10 Find $4 / 10$ of 10 . What do you notice? Can you write any other similar statements? | Odd one out. <br> Which is the odd one out in each of these trio <br> What do you notice? <br> Find $4 / 6$ of 24 <br> Find $2 / 3$ of 24 <br> What do you notice? Can you write any other similar statements? | Odd one out. <br> Which is the odd one out in each of these collections of 4 fractions <br> Why? <br> What do you notice? <br> Find $30 / 100$ of 200 <br> Find $3 / 10$ of 200 What do you notice? Can you write any other similar statements? | Odd one out. <br> Which is the odd one out in each of these collections of 4 fraction <br> $3 / 4 \quad 9 / 12 \quad 26 / 36$ <br> 18/24 <br> $\begin{array}{llll}4 / 20 & 1 / 5 & 6 / 25 & 6 / 30\end{array}$ <br> Why? <br> What do you notice? <br> $8 / 5$ of $25=40$ <br> $5 / 4$ of $16=20$ $7 / 6 \text { of } 36-42$ <br> Can you write similar statements? |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ordering <br> Put these fractions in the correct order, starting with the smallest. 1/2 1/4 1/3 | Ordering <br> Put these fractions in the correct order, starting with the smallest. 4/8 3/4 1/4 | Ordering <br> Put these numbers in the correct order, starting with the smallest. $1 / 40.755 / 10$ <br> Explain your thinking | Ordering <br> Put these numbers in the correct order, starting with the largest. $7 / 10,0.73,7 / 100,0.07371 \%$ | Ordering <br> Which is larger, $1 / 3$ or 2/5? <br> Explain how you know. |

## Fractions - Calculations

| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | add and subtract fractions with the same denominator within one whole (e.g. ${ }^{5} / 7+1 / 7$ $=6 / 7$ ) | add and subtract fractions with the same denominator | add and subtract fractions with the same denominator and multiples of the same number | add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions |



|  |  | Can you make up a similar pattern for eighths? <br> The answer is $5 / 10$, what is the question? (involving fractions / operations) | Can you make up a similar pattern for addition? <br> The answer is $3 / 5$, what is the question? <br> What do you notice? $\begin{aligned} & 11 / 100+89 / 100=1 \\ & 12 / 100+88 / 100=1 \\ & 13 / 100+87 / 100=1 \end{aligned}$ <br> Continue the pattern for the next five number sentences | Can you make up a similar pattern for subtraction? <br> The answer is $12 / 5$, what is the question | Another and another Write down 2 fractions with a total of $34 / 5$. ... and another, ... and another, .. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Continue the pattern $\begin{aligned} & 1 / 4 \times 3= \\ & 1 / 4 \times 4= \\ & 1 / 4 \times 5= \end{aligned}$ <br> Continue the pattern for five more number sentences. <br> How many steps will it take to get to 3? <br> $5 / 3$ of $24=40$ <br> Write a similar sentence where the answer is 56 . <br> The answer is $21 / 4$, what is the question <br> Give your top tips for multiplying fractions. | Continue the pattern $\begin{aligned} & 1 / 3 \div 2=1 / 6 \\ & 1 / 6 \div 2=1 / 12 \\ & 1 / 12 \div 2=1 / 24 \end{aligned}$ <br> What do you notice? $1 / 2 \times 1 / 4=$ <br> The answer is $1 / 8$, what is the question (involving fractions / operations) <br> Give your top tips for dividing fractions. |


|  |  | solve problems that <br> involve all of the <br> above | solve problems <br> involving increasingly <br> harder fractions to <br> calculate quantities, <br> and fractions to divide <br> quantities, including <br> non-unit fractions <br> where the answer is a <br> whole number |
| :--- | :--- | :--- | :--- |



|  |  |  | Another and another <br> Write a decimal numbers (to one decimal place) which lies between a half and three quarters? <br> ... and another, ... and another, ... |  |  |  | Complete the table. <br> Another and another <br> Write a fraction with a denominator of one hundred which has a value of more than 0.75 ? <br> $\ldots$ and another,.. and another, ... |  |  | Complete the table. <br> Another and another <br> Write a unit fraction which has a value of less than 0.5 ? $\ldots$ and another, $\ldots$ and another, ... |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ordering <br> Put these fractions in the correct order, starting with the smallest. $\begin{array}{lll} 1 / 2 & 1 / 4 & 1 / 3 \end{array}$ | Ordering <br> Put these fractions in the correct order, starting with the smallest. $\begin{array}{lll} 4 / 8 & 3 / 4 & 1 / 4 \end{array}$ | Order <br> Put th <br> the c <br> startin <br> smalle <br> $1 / 4$ <br> Expla | se nu rect <br> with t. <br> 0.75 <br> you | mbers rder, he |  | Orde <br> Put <br> the <br> startin <br> 7/10 <br> $71 \%$ |  |  |  | wing rder the 0.8 | gest. |


| Decimals - Compare (inc Rounding) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
|  |  |  | compare numbers with the same number of decimal places up to two decimal places | read, write, order and compare numbers with up to three decimal places | identify the value of each digit in numbers given to three decimal places |
|  |  |  | Round decimals with one decimal place to the nearest whole number | Round decimals with two decimal places to the nearest whole number and to one decimal place | Solve problems which require answers to be rounded to specified degrees of accuracy |
| Reasoning Examples - Combined Operations |  |  |  |  |  |
|  |  |  | Missing symbol <br> Put the correct symbol <br> < or > in each box | Missing symbol <br> Put the correct symbol <br> < or > in each box | True or false? <br> In all of the numbers below, the digit 6 is |


|  |  |  | $3.03 \square$ 3.33 <br> $0.37 \square$ 0.32 <br> What needs to be added to 3.23 to give 3.53? <br> What needs to be added to 3.16 to give 3.2? | 4.627 $\square$ 4.06 <br> 12.317 $\square$ 12.31 <br> What needs tobe added to 3.63 to give 3.13? <br> What needs to be added to 4.652 to give 4.1? | worth more than 6 hundredths. <br> Is this true or false? Change some numbers so that it is true. <br> What needs to be added to 6.543 to give 7 ? <br> What needs to be added to 3.582 to give 5 ? <br> Circle the two decimals which are closest in value to each other. $\begin{array}{lllll} 0.9 & 0.09 & 0.99 & 0.1 & 0.01 \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Do, then explain <br> Circle each decimal which when rounded to the nearest whole number is 5 . <br> $\begin{array}{llll}5.3 & 5.7 & 5.2 & 5.8\end{array}$ <br> Explain your reasoning <br> Top tips Explain how to round numbers to one decimal place? | Do, then explain <br> Circle each decimal which when rounded to one decimal place is 6.2. <br> $\begin{array}{llll}6.32 & 6.23 & 6.27 & 6.17\end{array}$ <br> Explain your reasoning <br> Top tips <br> Explain how to round decimal numbers to one decimal place? Also see rounding in place value | Do, then explain <br> Write the answer of each calculation rounded to the nearest whole number $\begin{aligned} & 75.7 \times 59 \\ & 7734 \div 60 \\ & 772.4 \times 9.7 \\ & 20.34 \times(7.9-5.4) \end{aligned}$ <br> What's the same, what's different? <br> ... when you round numbers to one decimal place and two decimal places? |

$\left.\begin{array}{|l|l|l|l|l|l|}\hline & & & \begin{array}{l}\text { Also see rounding in } \\ \text { place value }\end{array} & \\ \hline \text { place value rounding in } \\ & \begin{array}{l}\text { Ordering } \\ \text { Put these fractions in } \\ \text { the correct order, } \\ \text { starting with the } \\ \text { smallest. } \\ 1 / 2 \quad 1 / 4 \quad 1 / 3\end{array} & \begin{array}{l}\text { Ordering } \\ \text { Put these fractions in } \\ \text { the correct order, } \\ \text { starting with the } \\ \text { smallest. } \\ 4 / 8 \quad 3 / 4 \quad 1 / 4\end{array} & \begin{array}{l}\text { Ordering } \\ \text { Put these numbers in } \\ \text { the correct order, } \\ \text { starting with the } \\ \text { smallest. } \\ 1 / 4 \quad 0.75 \quad 5 / 10 \\ \text { Explain your thinking }\end{array} & \begin{array}{l}\text { Ordering } \\ \text { Put these numbers in the } \\ \text { correct order, starting } \\ \text { with the largest. } \\ 7 / 10,0.73,7 / 100,0.073 \\ 71 \%\end{array} \\ \text { amounts in order, starting } \\ \text { with the largest. } \\ 23 \%, 5 / 8,3 / 5,0.8\end{array}\right\}$

| Decimals - Calculations and Problems |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
|  |  |  | find the effect of dividing a one- or twodigit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths |  | Associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. 3/8) |
|  |  |  | solve simple measure and money problems involving fractions and decimals to two decimal places. | Solve problems involving numbers up to three decimal places | multiply one-digit numbers with up to two decimal places by whole numbers |
|  |  |  |  |  | multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places |
|  |  |  |  |  | use written division methods in cases where the answer has up to two decimal places |



| Percentages - Recognise and calculate |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Year 1 | Year 2 | Year 3 |  |  |
|  |  |  | Year 5 <br> recognise the per cent <br> symbol (\%) and | rear 6 <br> recall and use <br> equivalences between |



